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# Laminar Burning Characteristics of Ethyl Propionate, Ethyl Butyrate, Ethyl Acetate, Gasoline and Ethanol Fuels

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## Abstract

Ethyl esters have been considered as promising second-generation biofuel candidates, due to the available production from low grade biomass waste. Furthermore, with desirable energy densities, emissions performance, low solubility and higher Research Octane Number (RON), ethyl esters have proven attractive as fuel additives or alternatives for gasoline. In this study, high-speed schlieren photography was used to investigate the laminar burning characteristics of three ethyl ester fuels: ethyl acetate, ethyl propionate, and ethyl butyrate, in comparison with gasoline and ethanol at different initial temperatures and a variety of equivalence ratios, with an initial pressure of 0.1 MPa in a constant-volume vessel. For the five fuels, the stretched flame speeds, the un-stretched flame speeds, Markstein lengths, Markstein number, laminar burning velocities and laminar burning flux were calculated and analysed using the outwardly spherical flame method. The results show that for all examined initial temperatures (60°C, 90°C and 120°C) and equivalence ratios; ethanol had the highest un-stretched flame propagation speeds, whilst ethyl acetate (EA) had the lowest. At high initial temperatures (120°C), it was observed that the un-stretched flame speed trends of ethyl propionate (EP) and ethyl butyrate (EB) proved faster compared to gasoline, especially for rich conditions. The EB and EA flames demonstrated greater stability when compared to ethanol, EP, and gasoline. Analysis showed that ethanol yielded the fastest flame velocities, whilst EA consistently had the lowest among all the five fuels. The laminar burning velocities of the EP fuel were faster compared to EB and EA, whilst slower than ethanol and gasoline at 60°C. Further increase of the initial temperature, up to 120°C, showed the laminar flame speed of EP and EB to be faster than gasoline, indicating a fast-burning property, and potential of improving engine thermal efficiency.

**Keywords:** Ethyl acetate, ethyl propionate, ethyl butyrate, laminar burning velocity, schlieren optical method

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## 1. Introduction

With an ever present demand for energy worldwide combined with a growing population and reliance on fuel powered applications (expected to grow by 57% until 2030) [1], the dependency on the finite and diminishing supply of fossil derived fuels alongside the requirement for enhanced environmental consciousness had resulted in vast investment, interest and continuous investigation into the future generation of alternative fuels [2]. The prevalent interest in recent years considered the derivation, functionality and potential of biological fuels, i.e. biofuels, sourced from biomass, with only 3% currently being economically exploited [2]. As such, research efforts have been focussed towards achieving performance characteristics of equal measure to the current market (ethanol, gasoline and isooctane).

Bio-ethanol has been established as the prominent alternative to gasoline, being mass produced via alcohol fermentation, cementing its matured status (relative to other alternatives) within the bioenergy market [3, 4]. However, whilst bio-ethanol afforded a high volume of production, it resulted in a large energy consumption during processing, negating the benefits of its use as a primary fuel or component blend additive [1, 5]. This was supported by unfavourable physical attributes, including: a low energy density (high gravimetric oxygen content), high volatility, and high solubility (fuel quality affected by atmospheric water content, affecting its long term stability) [6].

More recently, breakthroughs in mass production technologies broadened the spectrum of alternative fuels sourced from biomass, with research into the flame and spray characteristics of fructose derived 2-methylfuran (MF) and 2,5-dimethylfuran (DMF) yielding favourable results, with the fuels also exhibiting desirable properties such as: high energy density (close to gasoline and between 30–40% greater than ethanol), insolubility (high stability), high boiling point (less volatile), high research octane number (RON) (increased efficiency and resistance to auto-ignition), and low energy consumption during production [5-8]. Furthermore, investigations into second generation ester biofuels showed a reduction in production complexity, thereby improving the efficiency of the necessary conversion steps (dictated by the engine specific fuel characteristics), yielding high grade fuels without detriment to the net energy balance [9-12].

Due to the lower production cost for esters in the dual fermentation bio-refinery (DFB) process, a series of ester oxygenates was evaluated recently for use as gasoline octane providers. It was found that EP, EB and EA as gasoline additives provided a significant increase in the mean octane rating without a drastic change in vapor pressure [13]. Ethyl ester fuels had several advantages over ethanol and ethers. First, they were not toxic. Second, they had pleasant odor. Third, lower exhaust emissions of carbon monoxide, aldehydes and ketones were expected because of the higher oxidation state of the esters [14]. Jenkins et al. [10] concluded that the ester fuels were completely miscible with gasoline, enabling 50:50 blends, i.e. fuel integration instead of replacement, with EA best suited to SI applications (low melting and flash point).

As an extension of the ester fuels application in spark ignition/compression ignition (SI/CI), research into Homogeneous Charge Compression Ignition (HCCI) was conducted by Contino et al. [11-12] which concluded that EA, EP and EB had a slower ignition rate than ethanol (agreed by Jenkins et al.) [10]. Furthermore, it was shown that the esters offered no loss of power (energy content of stoichiometric mixtures were similar to ethanol), with an improved mixture preparation (greater enthalpies of vaporisation), and good overall stability at various equivalence ratios. Contino et al. [9] also investigated the engine performance and emissions of methyl and ethyl valerates in SIE and found that the esters had a higher flame speed compared to Primary Reference Fuels (PRF95). Moreover, no significant difference was observed for emissions and performance when the engine was running with pure esters compared to PRF95.

Table.1. shows the general properties of the proposed fuels for baseline evaluation with ethanol and gasoline. It was noticed that the three fuels demonstrated a reduction in LHV relative to gasoline (20–30% less, due to their oxygen content which itself offered reduced soot formation), but an increase compared with ethanol (10–20% for EP and EB). Furthermore, EP and EB exhibited similar boiling properties (98.89–120°C) and solubility (low) to that of gasoline, benefitting from reduced volatility and high stability, whereas EA demonstrated properties akin to ethanol, displaying an elevated RON (116) to accommodate higher compression ratios and cycle efficiencies. Collectively, the fuels displayed latent heat of vaporisation similar to gasoline, with flash points indicating potential diversity in application: EA (-2.78°C) in SI; EP and EB (12.22–18.89°C) in HCCI, thereby cementing their combustion credentials [10].

The present paper aims to analyse and evaluate the laminar flame speed of three ester biofuels, namely: ethyl acetate (EA), ethyl propionate (EP), and ethyl butyrate (EB), against gasoline and ethanol. Laminar flame

propagation characteristics are important fundamental physicochemical properties of a fuel–air mixture for validating the chemical reaction mechanisms and gaining a better understanding of the combustion process in engines [15, 16]. This study forms part of a series of experiments to explore the use of ethyl esters as additive or surrogate fuel for gasoline in SIE, utilising schlieren photography to investigate the laminar flame speed, Markstein length, Markstein number, laminar burning velocity and burning flux at different initial temperatures.

**Table.1.** General Properties of the research fuels (EA, EP, EB, ethanol and gasoline)

	<b>Ethyl Acetate (EA)</b>	<b>Ethyl Propionate (EP)</b>	<b>Ethyl Butyrate (EB)</b>	<b>Ethanol</b>	<b>Gasoline</b>
Linear structure formula	$\text{CH}_3\text{COOC}_2\text{H}_5$	$\text{CH}_3\text{CH}_2\text{COOC}_2\text{H}_5$	$\text{CH}_3\text{CH}_2\text{CH}_2\text{C}(\text{O})\text{OC}_2\text{H}_5$	$\text{CH}_3\text{OCH}_3$	Variable
Molecular formula	$\text{C}_4\text{H}_8\text{O}_2$	$\text{C}_5\text{H}_{10}\text{O}_2$	$\text{C}_6\text{H}_{12}\text{O}_2$	$\text{C}_2\text{H}_6\text{O}$	$\text{C}_2$ to $\text{C}_{14}$
H/C ratio	2.00	2.00	2.00	3.00	1.95
O/C ratio	0.50	0.40	0.33	0.50	0.02
Molecule schematic					Variable
Molecular mass (kg/kmol)	88.10	102.00	116.00	46.07	100–105
Gravimetric oxygen content (%)	36.36	31.37	27.59	34.78	2.35
Density @ 20 C (kg/m <sup>3</sup> )	897	891	886	794.00	744.60
Water solubility	High	Low	Low	High (>100mg/ml @73°F)	Insoluble
Boiling point (°C)	77.22	98.89	120.00	77.30	96.30
Flash point (°C)	-2.78	12.22	18.89	17.22	-42.7
Research octane number (RON)	116.00	–	–	110.00	96.80
Stoichiometric air-fuel ratio	7.80	8.74	9.46	8.25	14.13
LHV (MJ/kg)	23.79	26.53	28.64	26.90	42.90
LHV (MJ/L)	21.34	23.64	25.38	21.36	31.90

## 2. Experimental setup

### 2.1 Schlieren optical method

The laboratory setup for experimentation was a replication of the approach as detailed by Tian et al. [5] and Ma et al. [7] with Figure.1 providing a detailed schematic of the arrangement. As shown, a constant volume combustion vessel with two circular quartz observation windows (100 mm diameter) was utilised, alongside eight heating elements, installed at each corner. Temperature modulation of the vessel was implemented via closed loop control, to monitor the heating elements described and allow continuous observation of the fuel-air mixture condition within the chamber. The fuel injection strategy was fulfilled through a gasoline direct

injection (GDI) nozzle, which was mounted in the top cover of the vessel, and was driven by an ECU-computer system. Finally, to achieve the necessary spark for ignition, a pair of tungsten electrodes was positioned in the centre of the vessel, with a pressure release valve featured for safety purposes, operating at 0.7 MPa.

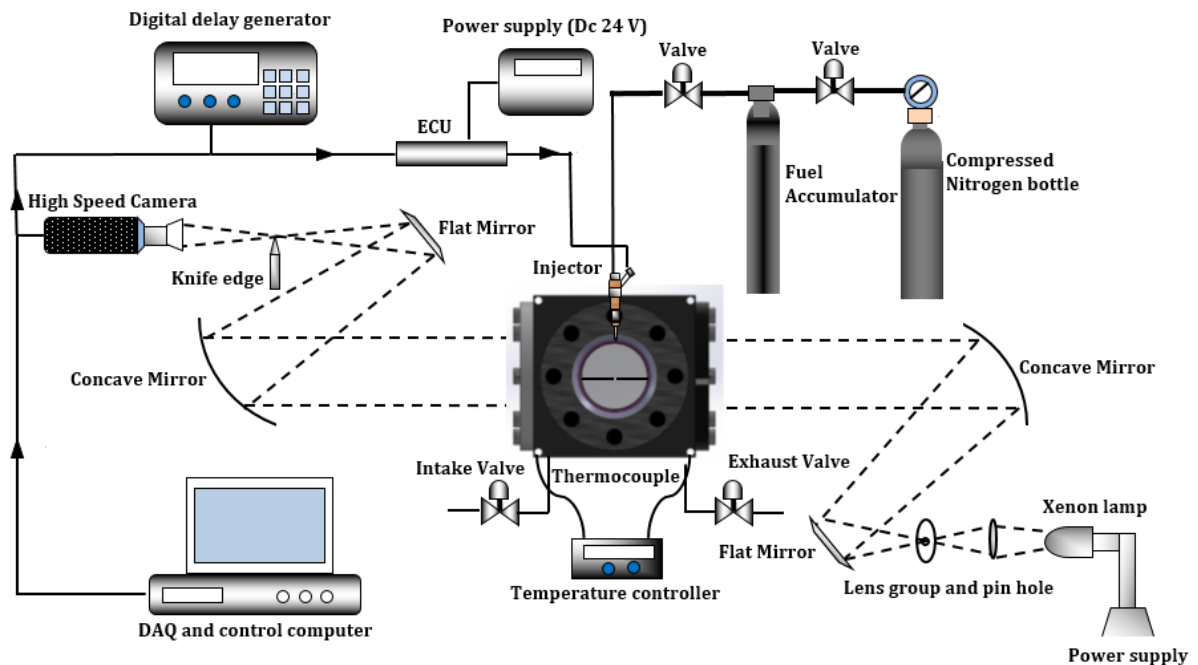


Figure.1. Schematic diagram for schlieren set up

To begin experimentation, a point light source was generated, utilising a 500 W xenon lamp combined with a lens array, prior to an adjustable aperture. This light source was directed at a concave mirror to yield a parallel beam, which passed through the vessel chamber via the aforementioned observation windows, illuminating the test environment. Following this, the parallel beam was then collected at a second concave mirror on the opposite side of the vessel, which integrated the light prior to its intersection by a knife edge, to achieve the desired schlieren effect (two dimensional imaging). To document the combustion events, a Phantom research V710 high-speed camera was utilised (synchronised with spark timing; no recorded delay), with a capture rate of 10 kHz (10,000 frames per second) and resolution of 800 x 800 pixels.

Compressed air was used to scavenge the burned gases in the exhaust. After flushing and before each test, the vessel chamber was opened to the ambient air until the air temperature inside the vessel stabilized at the test point. Once the temperature stabilized, the valves to the chamber were closed and the fuel was injected to form a homogenous fuel-air mixture, remaining undisturbed for a minimum of five minutes to guarantee homogeneity and a relative state of inactivity. Following this, the mixture was ignited via electrode spark, which

simultaneously switched the camera on to record. After the combustion event, the burned products were extracted from the vessel chamber, enabling the experiment to be restarted. To ensure confidence in procedure, each test was repeated a minimum of three times, with the process being pursued at initial temperatures of 60°C, 90°C and 120°C and a variety of  $\phi$  from 0.8 to 1.4.

### 3. Image processing

Following experimentation, the captured schlieren images were analysed via an in-house MATLAB program, to evaluate the basic laminar flame characteristics. To eliminate the negative influence of factors including spark ignition and flame quenching during such analysis, the flame radii were measured in four directions at an inclined angle of 45° relative to the electrodes (see Figure. 2). The captured images were 8-bit grayscale images. The images were processed using the following steps. Firstly, the raw flame images were background corrected using a frame prior to the start of the flame. This step eliminated any background noise. Then, a threshold of 5% was used to convert the background corrected image to a binary image. Finally, the boundary of the flame area can be detected based on the binary image. Observation of the flame radius was isolated to the vertical and horizontal directions, in the range of 6–25 mm, as deemed sufficient by previous studies [5, 7]. All results in the analysis were then averaged from the three tests, as discussed.

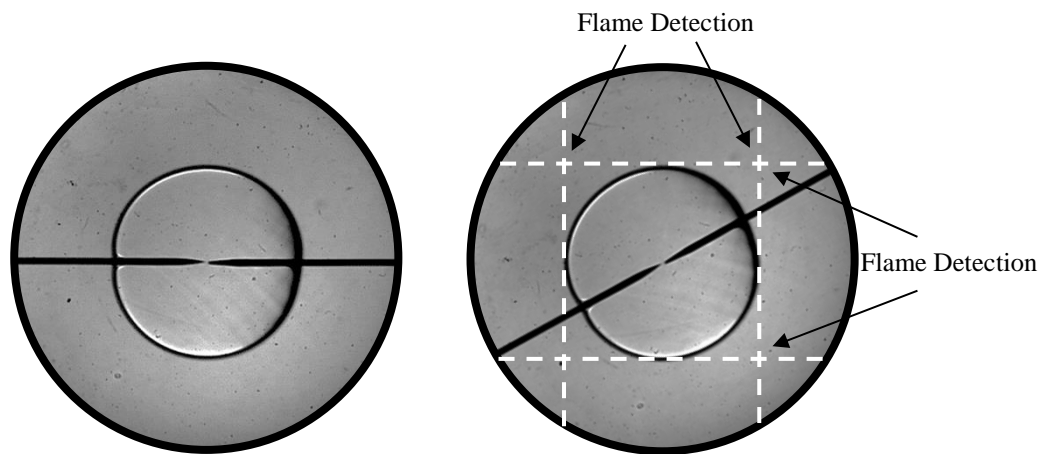


Figure.2. Laminar flame radius detection (left: original image; right: 45° rotated image)

To evaluate the laminar burning velocities, various parameters required definition, with the first being the instantaneous rate of change of the flame radius ( $r_u$ ), namely the stretched laminar flame speed ( $S_n$ ):

$$S_n = \frac{dr_u}{dt} \quad (1)$$

where  $t$  was the time after ignition. By knowing the stretched laminar flame speed, the stretch rate ( $\alpha$ ) was calculated by [17, 18]:

$$\alpha = \frac{2S_n}{r_u} \quad (2)$$

The linear correlations between the stretch rate and flame speed were expressed by [17, 18]:

$$S_n = S_s - L_b \times \alpha \quad (3)$$

where  $S_s$  represented the un-stretched flame speed, and  $L_b$  expressed the Markstein length. Determination of  $S_s$  was achieved by extrapolating  $S_n$  to a zero stretch rate, whilst  $L_b$  was the negative value of the gradient of the flame propagation speed against the stretch rate curve.

The laminar burning velocity ( $u_1$ ) could be obtained from the equation [17, 18]:

$$u_1 = S_s \times \frac{\rho_b}{\rho_u} \quad (4)$$

where  $\rho_b$  and  $\rho_u$  were the burned and unburned mixture densities, respectively. Assuming the pressure was constant, the burned ( $\rho_b$ ) and unburned gas densities ( $\rho_u$ ) could be found from the conservation of mass equation:

$$\frac{\rho_b}{\rho_u} = \frac{V_u}{V_b} = \frac{n_u T_u}{n_b T_b} \quad (5)$$

where  $n_u$  and  $n_b$  were the number of moles of reactants and products, and  $T_u$  and  $T_b$  were the initial and adiabatic flame temperatures.

The adiabatic flame temperatures were calculated using HPFLAME [19], which incorporates the Olikara and Borman equilibrium routines [20].

The flame thickness was calculated by the ratio of kinematic viscosity to laminar flame velocity via [21, 22]:

$$\delta_L = \frac{\nu}{u_1} \quad (6)$$

The Markstein number was calculated from the ratio of Markstein length to the flame thickness [17]:

$$M_a = \frac{L_b}{\delta_L} \quad (7)$$

The laminar burning flux, which reveals the eigenvalue of the flame propagation, was calculated by [17]:

$$f = u_1 \times \rho_u \quad (8)$$



## 4. Results and discussion

### 4.1. System validation

In order to validate the system setup and procedures used, laminar burning velocities of ethanol-air mixtures at 0.1MPa initial pressure and 363 K initial temperature were calculated and compared with available data from published literature. Figure.3 indicates that the current measurement proved consistent with available data, and demonstrated good agreement with the widely accepted result of Bradley et al. [23], and in addition, Liao et al. [24]. This validates the present experimental setup and methodology.

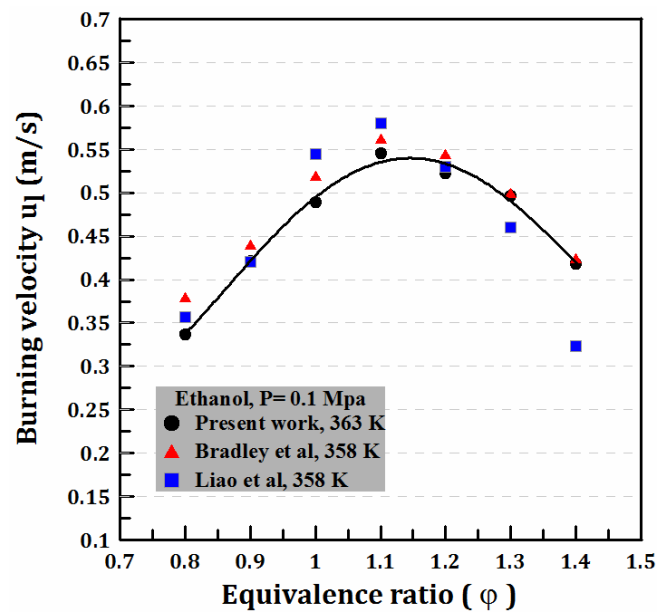
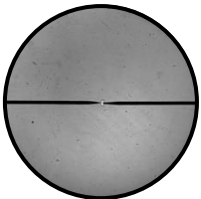
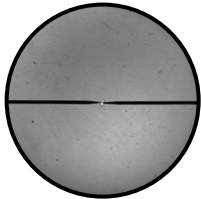
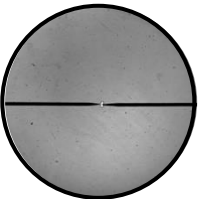
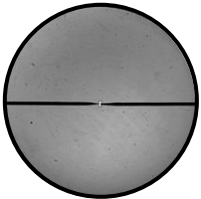
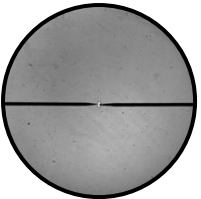
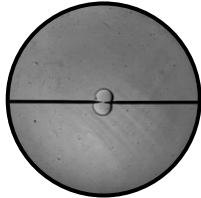
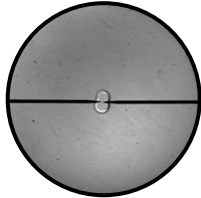
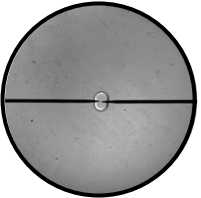
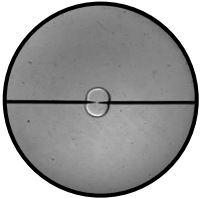
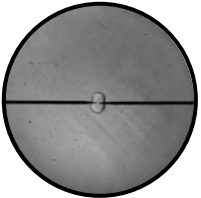
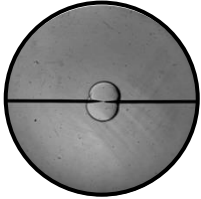
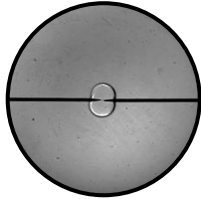
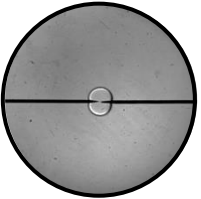
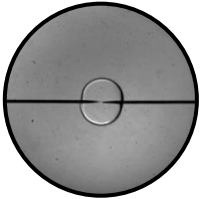
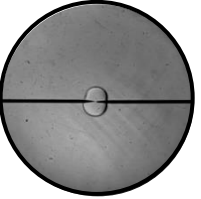
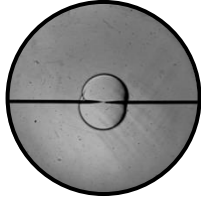
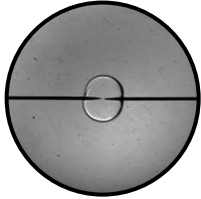
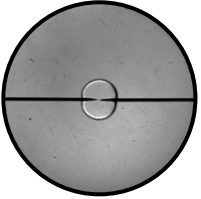
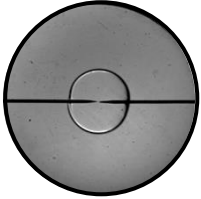
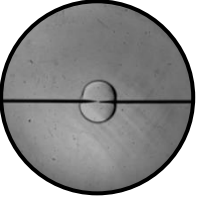
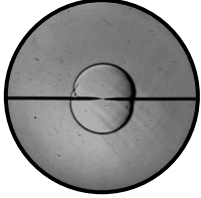
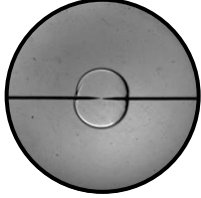
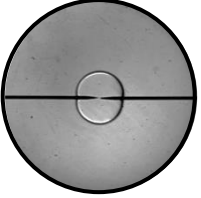
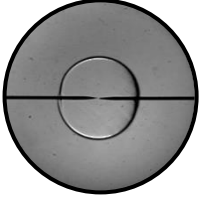
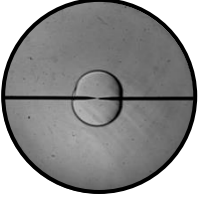
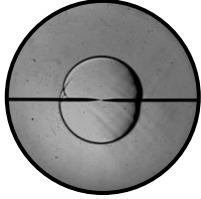
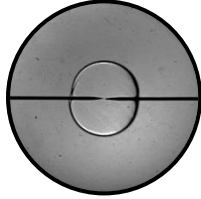
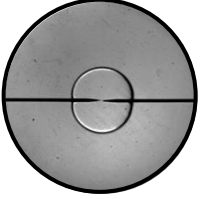
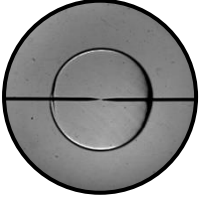
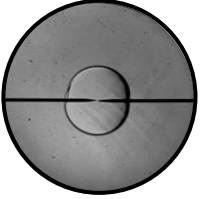
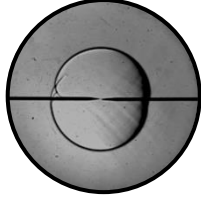
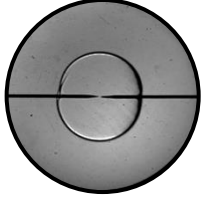
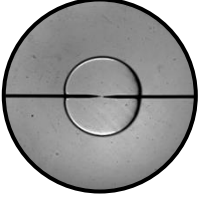
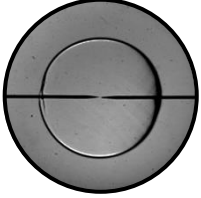
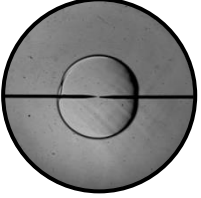
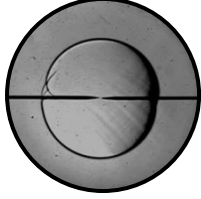
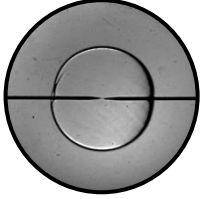
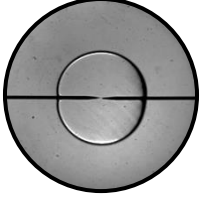
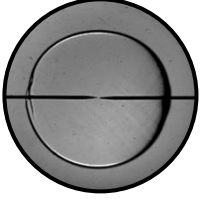
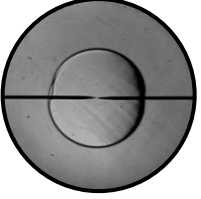


Figure.3. Laminar burning velocity of ethanol at 0.1 MPa and 363K in this work, compared with [23, 24]

### 4.2. Flame morphology

Figure.4 demonstrates the time elapsed flame propagation of the five fuels at stoichiometric conditions with an initial temperature of 90°C and an initial pressure of 0.1 MPa. As shown, ethanol exhibited the greatest flame propagation speeds among the five fuels, whilst EA displayed the lowest. EP proved slower than ethanol, but faster than gasoline. EB was almost comparable with gasoline. As the flames approached the vessel wall, the spherical profiles became distorted, with a flatter surface on the upper side due to the influence of the internal vessel geometry [25]. Due to the quenching effect of the electrodes, all flame propagation speeds were slower along the direction of the electrodes than in the vertical direction, thus the flame was not perfectly spherical. The wrinkling near the electrodes was attributed to the quenching effect. All images used for calculation were chosen such that significant wrinkling on the flame front surface (which may affect the results), was avoided.

Time elapsed	EP	EB	EA	Ethanol	Gasoline
1 ms					
2.5 ms					
4 ms					
5.5 ms					
7 ms					
8.5 ms					
10 ms					
11.5 ms					

194

195 [Figure.4.](#) Flame images of stoichiometric fuel-air mixtures at initial temperature of 90°C and ambient pressure

#### 4.3.1. Stretched flame propagation speed

The stretched flame propagation speed versus stretch rate (marked as  $\alpha$ , in the figures) for the five fuels at different equivalence ratios under 120°C are given in Figure.5. During the early stages of flame propagation (when the flame radius was small), the stretch rate of flame front surface was large and the flame propagation speed proved low. As the flame propagated outwardly, the flame stretch rate decreased and the flame propagation speed increased. Removal of data affected by ignition energy and the electrodes during the early stage of flame development yielded a linear correlation for the stretched flame speed and the flame stretch rate as shown in Figure.5. The linear correlation between the flame stretch rate and the flame radius at a large stretch rate was considered representative of the laminar flame characteristics [5]. However, in some cases, non-linearity appeared at large stretch rates. For instance, at  $\phi=1$  for gasoline and EP, the results showed a bending trend at maximum stretch rates. In order to evaluate the un-stretched flame speed and Markstein length correctly, those points deemed too far from linearity were removed as poor data. This was enforced by a deviation constraint of less than 5% required for the fitting result, with the offset to the fitting line of the individual points also restricted to within 5%, whilst retaining as many data points as practicably possible.

Recently, the nonlinear correlation is used to process the data, especially for the lean and rich mixtures. Li et al. [26] demonstrated the comparison of laminar flame speeds with linear and nonlinear methodologies for n-Pentanol-air mixtures at various initial conditions. They revealed that the results yielded in the two methods were closely matched at all conditions with a slight difference for lean and rich mixtures. However, the differences between the two groups of data were smaller than  $2 \text{ cm}\cdot\text{s}^{-1}$ , within the uncertainty of measurements. Therefore, for this study the linear methodology is used for the laminar flame speeds calculations.



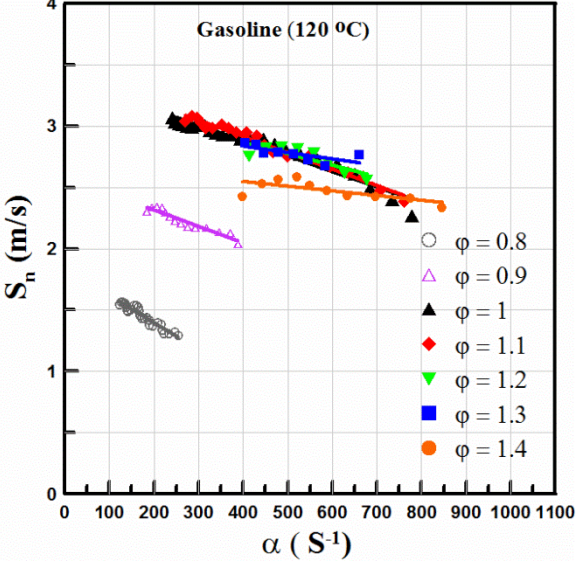
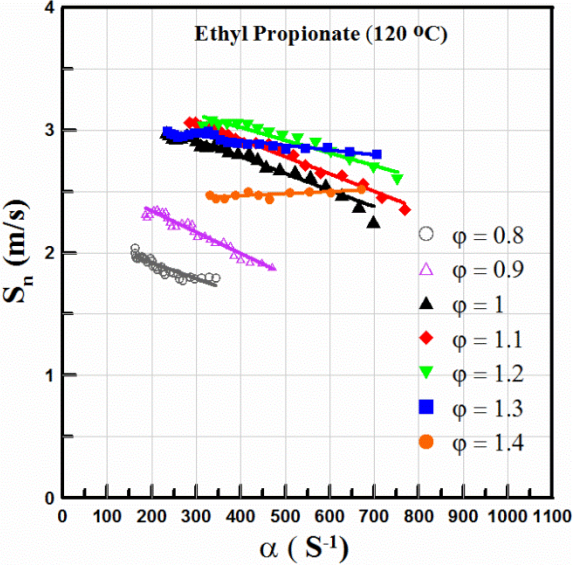
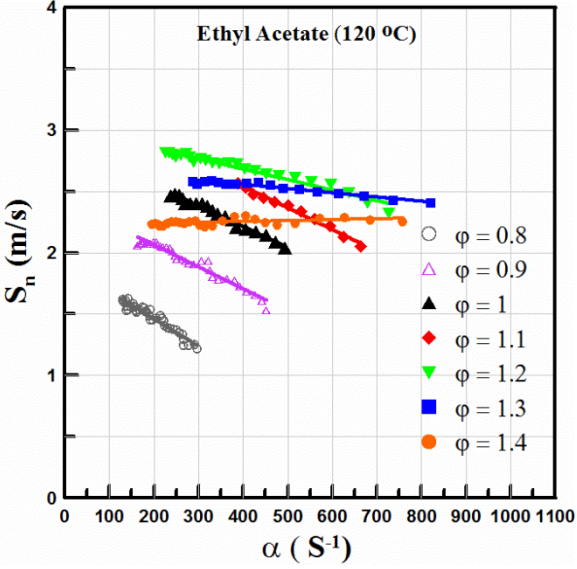
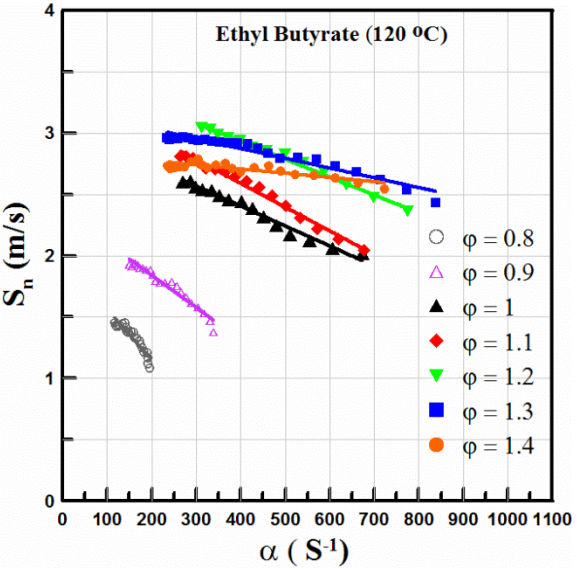
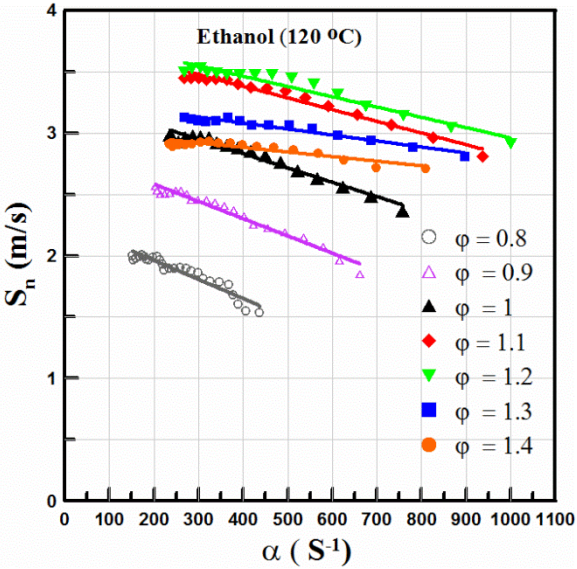


Figure 5: Stretched flame speed of the test fuels at 120°C initial temperature at different equivalence ratios and stretch rates.

### 4.3.2. Un-stretched flame propagation speed

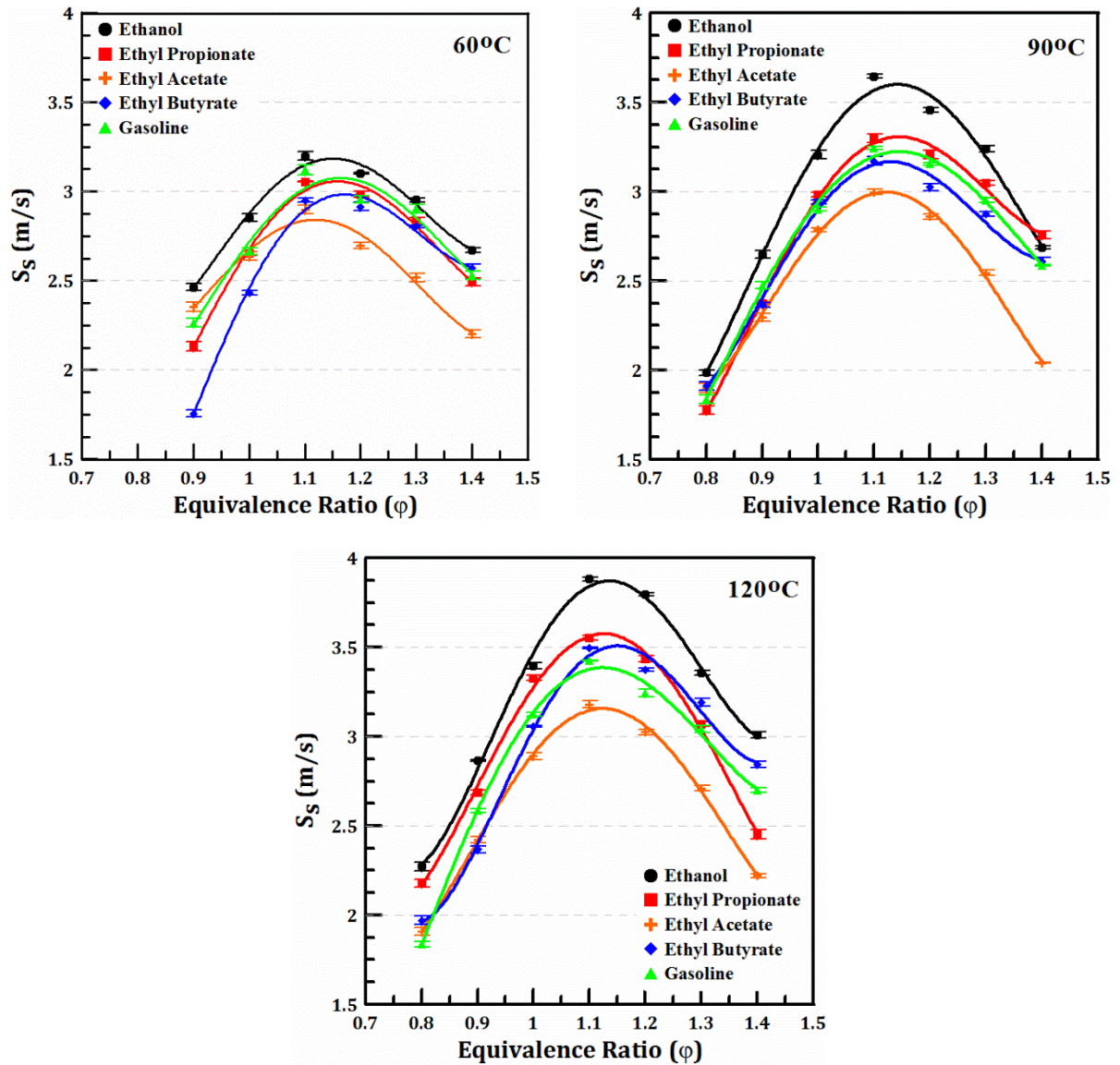
The un-stretched flame propagation speeds were obtained by extrapolating the fit line of the stretched flame propagation speeds to a zero stretch rate ( $\alpha = 0$ ), whilst the Markstein lengths were determined by calculating the gradient of the stretched flame propagation speed, utilising the stretch rate slope in the linear range. Figure.6 details the un-stretched flame speeds of the five fuels at different initial temperatures and equivalence ratios. The scattered points indicate the experimental results, whilst the solid lines are quadratic fit curves. The un-stretched flame propagation speed was increased with an increase of the initial temperature due to enhanced chemical reaction rate.

For all examined initial temperatures (60°C, 90°C and 120°C) and equivalence ratios, ethanol had the highest un-stretched flame propagation speeds, whilst EA had the lowest. The highest un-stretched flame speed for ethanol could be due to its molecular structure, which consisted of hydroxyl functional group (-OH) attached to the terminal carbon atoms, leading to a higher un-stretched flame propagation speeds compared to the other fuels [27]. The un-stretched flame speeds of the ethyl ester fuels showed promise when compared with gasoline, especially in the case of EP and EB. At an initial temperature of 60°C, the un-stretched flame speed trend of EP was almost identical to that of gasoline, whilst EB proved lower. However, at high initial temperatures (90°C and 120°C), when compared with gasoline, the trend of EP was greater, whilst EB was faster in rich conditions at 120°C. This is evident at 120°C, where the maximum un-stretched flame propagation speeds of EP and EB were approximately 0.13 m/s and 0.07 m/s respectively, showing an increase relative to gasoline. For the five tested fuels, the peak un-stretched flame speeds occurred in slightly rich mixtures when the equivalence ratio was between 1.0 and 1.2, as expected.

In contrast to EP and EB, as the initial temperature was increased, the difference between the un-stretched flame propagation speeds of EA and gasoline was also increased. It was noticed that at 60°C the maximum un-stretched flame speed of EA was 0.22 m/s slower than gasoline, whilst at 120°C it was 0.25 m/s.

The minimum un-stretched flame propagation speeds for EA compared with EP and EB could be due to dissociation bond energies of C-H. EA had the minimum inner C-H bond compared to EP and EB, therefore EA gives the smallest laminar burning velocity. Also, EA displayed higher sensitivity to the water formation which slower its un-stretched flame speed compared to EP and EB [27, 28].





**Figure.6.** Un-stretched flame speed of the test fuels at different temperatures and equivalence ratios (a) 60°C, (b) 90°C and (c) 120°C.

#### 4.3.3. Markstein length, flame thickness and Markstein number

The Markstein length indicates the influence of stretch rate on flame propagation speed, which characterizes the diffusion-thermal instability [15, 29]. Normally, the Markstein length decreases as the equivalence ratio increases for heavy hydrocarbon–air mixtures, whilst the opposite trend is expected for light hydrocarbon–air mixtures [30]. Figure.7 demonstrates the influence of fuel/air equivalence ratio and initial temperature on the flame/stretch interaction of the five fuels and the burned gases, with the Markstein length ( $L_b$ ) quantifying the effect. Generally, the Markstein lengths decreased monotonously with increasing equivalence ratio for each initial temperature. This was because all the tested fuels were heavy hydrocarbon-air mixtures, and the

Markstein length depends on the Lewis number of the fuel for a lean mixture, or that of oxidizer for a rich mixture [30].

For all examined initial temperatures, the Markstein length of EB was the highest among the five fuels, and therefore demonstrated the most stable flame characteristic at the tested condition. EA followed EB in terms of flame stability, exhibiting higher Markstein lengths for  $\phi \leq 1.1$ , especially at initial temperatures of 60°C and 90°C. The Markstein length of ethanol proved to be the smallest among the five fuels, and therefore had the most unstable flame characteristic at the tested condition. Positive Markstein lengths suggested that the flame speed decreases with an increase in the stretch rate, whilst negative Markstein lengths indicated that the flame speed increases with an increase in the stretch rate. Each of the fuels had lower flame speeds when the stretch rate was increased, except EA at  $\phi=1.4$ , with the negative values of the Markstein length concluding that the EA flame was more unstable at the examined temperatures under rich conditions. Bradley et al. [17] postulated that if the Markstein length is larger than 1.5, the flame will be initially stable until a critical flame radius is reached. This means that EB and EA demonstrate better initial flame stabilities than EP in a lean burning condition. Among the five fuels, EP and ethanol had the weakest initial flame stabilities at different initial temperatures.

With regards to temperature, the Markstein lengths exhibited higher values at low equivalence ratios ( $\phi = 0.8-0.9$ ) when the initial temperature was 60°C, and decreased as the initial temperature was increased. This suggests that rich mixtures and/or high initial temperature lead to instability of the flame front, as the diffusively-thermal stability of lean ethanol–air mixtures was stronger than that of rich mixtures. With respect to the initial temperature, the Markstein length of EB at the lean mixture of  $\phi=0.9$  decreased as the temperature increased, with a 31.6% reduction from 3.8mm to 2.6mm. For stoichiometric and rich conditions, the difference in Markstein length of EB was small as the initial temperature increased. The Markstein length for EA decreased as the temperature increased for almost all equivalence ratios, and proved less sensitive to the change of the initial temperature.

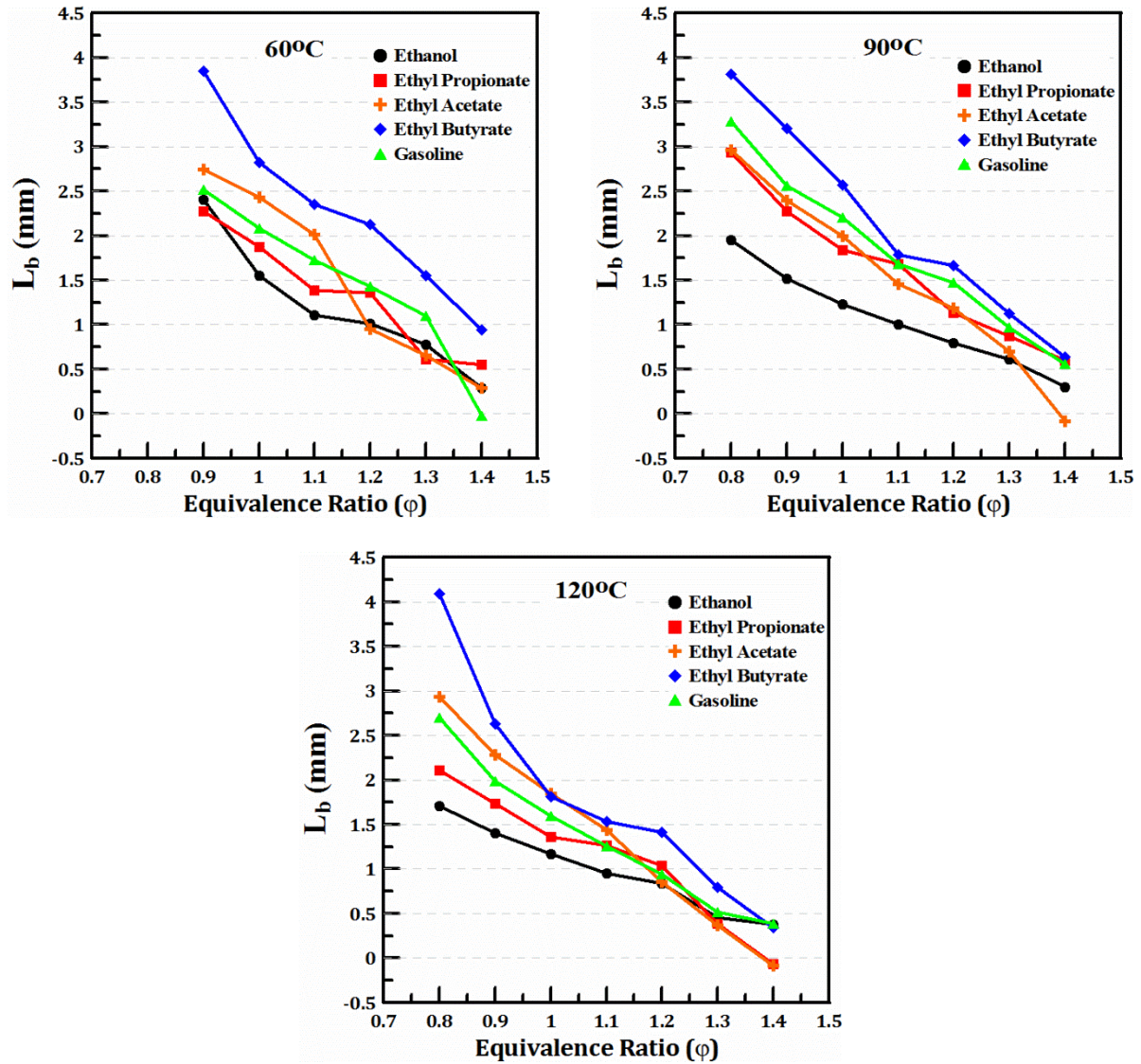


Figure.7. Markstein length of test fuels at different temperatures and equivalence ratios (a) 60°C, (b) 90°C and (c) 120°C.

Two kinds of flame surface instabilities acted on the flame front: the diffusion-thermal instability and the hydrodynamic instability [15, 31]. The Markstein length was used to characterize the diffusion-thermal instability, whilst the hydrodynamic instability was determined by the density transition across the flame front, being represented by the flame thickness and the density ratio. Flame thickness had an inhibiting effect on hydrodynamic instability, i.e. as the flame thickness decreased, the flame surface instability increased.

Figure.8 shows the flame thickness versus equivalence ratio for each of the tested fuels at different initial temperatures. In general, all the five fuels demonstrated similar trends, with the minimum values occurring near  $\phi=1.1$ , indicating higher instability. For all examined initial temperatures, EA yielded the largest flame thickness among the five fuels at almost all the equivalence ratios, and therefore the lowest hydrodynamic instability. In



contrast to EA, ethanol had the lowest flame thickness and consequently the highest hydrodynamic instability. A thinner flame usually indicates intensified combustion and faster flame speed, but it also results in lower tolerance to both internal and external disturbances, making the flame more vulnerable to destabilization. The results of EP, EB and gasoline proved comparable with each other across all equivalence ratios, and existed between the trends of EA and ethanol. For each of the five fuels, the flame thickness data was not sensitive to the variation of initial temperature, except for points around the limits of the lean and rich condition. This indicated that the initial temperature was not the most important parameter to affect the flame thickness, and thus the Markstein numbers were determined from the Markstein lengths for the same fuels.

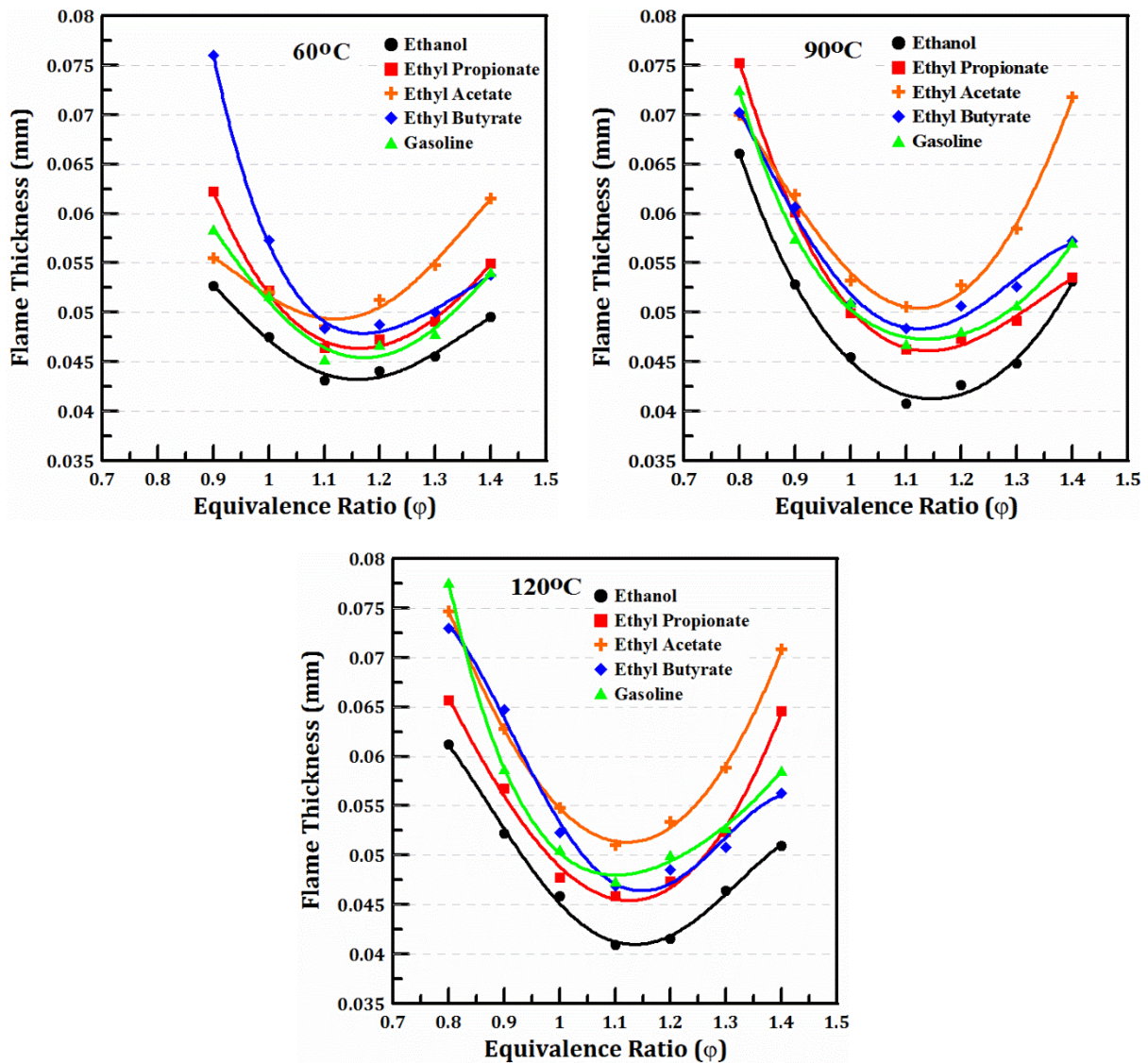


Figure.8. Flame thickness of the test fuels at different temperatures and equivalence ratios (a) 60°C, (b) 90°C and (c) 120°C.

The effect of local heat release on the flame morphology and the flame front curvature was determined by the Markstein number, which quantified the response of a laminar flame to stretch and could be used to indicate the stability of laminar and turbulent flame fronts. Figure.9 details the results of the Markstein number at different initial temperatures. Lean mixtures yielded high positive values, which decreased as the mixture became richer, proving similar to the result of the Markstein length. It was observed that the Markstein number of EB was the highest among the five fuels at the majority of the tested equivalence ratios. Ethanol followed by EP had the lowest Markstein numbers, which would increase the propensity of the flames to become less stable.

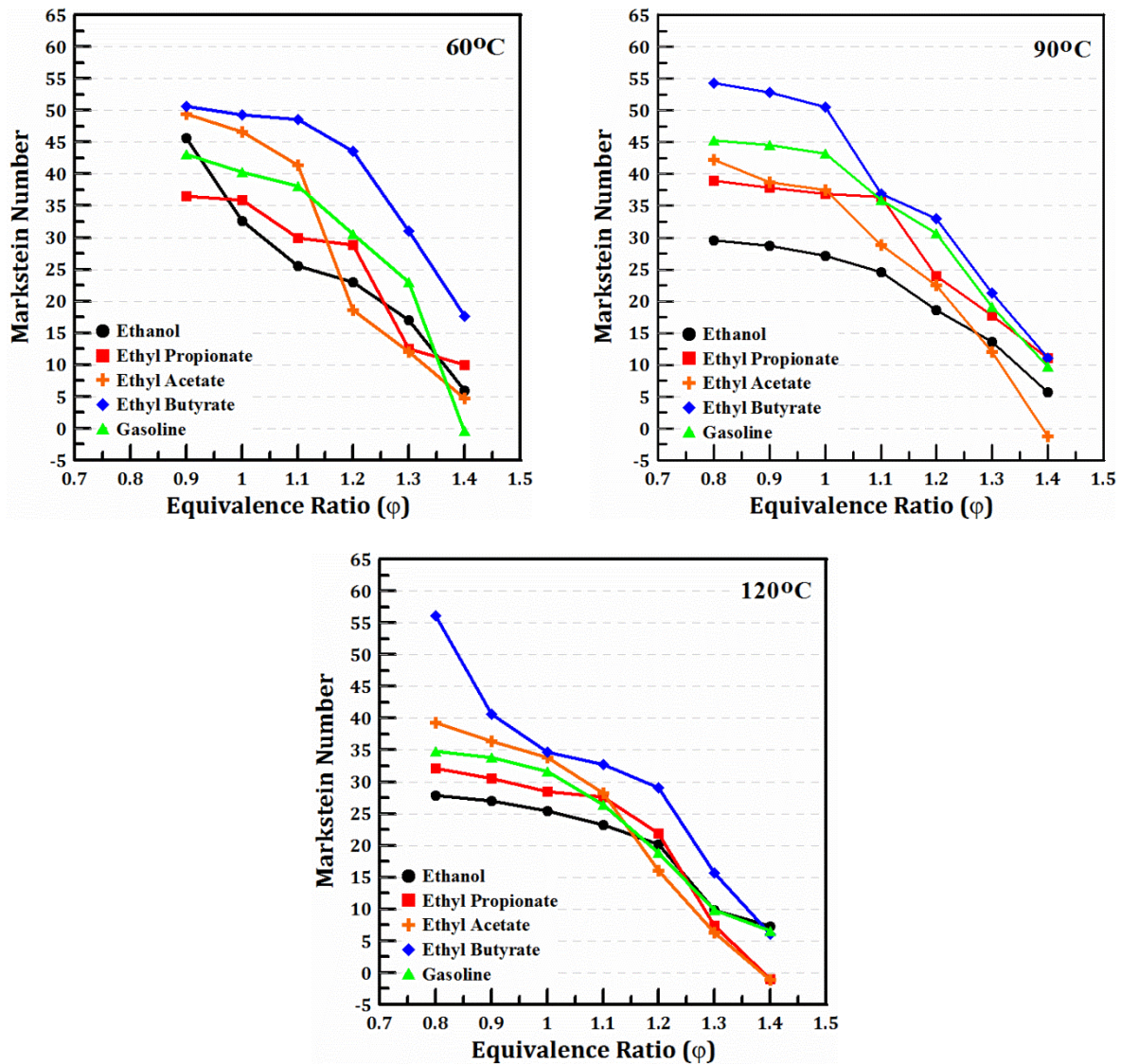


Figure.9. Markstein number of the test fuels at different temperatures and equivalence ratios (a) 60°C, (b) 90°C and (c) 120°C.

#### 4.4. Laminar burning velocities and burning flux

The laminar burning velocity was considered a strong function of the equivalence ratio and initial temperature of the reactants [32]. It was defined as the speed at which the flame front was moving towards the unburned mixture. Figure.10 shows the laminar burning velocities versus the equivalence ratios at different initial temperatures. The laminar burning velocities of the five fuels under varying initial temperatures exhibited peaks near the equivalence ratio of 1.1, which correlated to the state of the un-stretched flame speeds. Observation of the five fuels across all examined initial temperatures showed ethanol to yield the highest burning velocity, whilst ethyl acetate had the lowest. Furthermore, it was evident that the laminar flame speeds of the ethyl ester fuels in order of decreasing value were: ethyl propionate (EP) > ethyl butyrate (EB) > ethyl acetate (EA), in general for almost all tested equivalence ratios.

For the three ethyl esters examined, the experimental data indicated that the burning velocity increased between  $\phi = 0.8$  and 1.1, at which a maximum value was observed at different initial temperatures, before decreasing at higher equivalence ratios. Moreover, at an initial temperature of 60°C the maximum burning velocity between the ethyl ester fuels proved similar (at 0.1 MPa bar, 41.2 cm/s for EP, 39.6 cm/s for EB and 39.4 cm/s for EA). However, at higher initial temperatures (specifically 120°C), the maximum remained close between EP (55.7 cm/s) and EB (54.52 cm/s), but not when compared with EA (50.1 cm/s).

In comparison with gasoline, the laminar burning velocity of the three ethyl esters showed a competitive velocity profile, especially in the case of EP and EB. For the initial temperature of 60°C, gasoline was more closely matched by EP, although the laminar burning velocity of EP was marginally lower. The maximum burning velocity for gasoline was 42.3 cm/s, whilst for EP it was 41.2 cm/s (a decrease of 2.6%). As the initial temperature was increased to 90°C, the laminar flame speed of EP was matched with that of gasoline, except for rich conditions, with EP proving slightly higher. Further increase of the initial temperature to 120°C resulted in the burning velocity profile of EP to be greater than gasoline. The maximum burning velocity for EP was 55.7 cm/s, whilst for gasoline it was 54 cm/s (an increase of 3.2%). For the EB burning velocity, it was noted that as the initial temperature increased, the laminar velocity profile became closer to that of gasoline, especially at 120°C where the EB laminar velocity profile proved higher compared to gasoline, especially for rich conditions. The maximum burning velocity for EB was 54.52 cm/s, whilst for gasoline it was 54 cm/s (an increase of 1.0%).



In contrast to EP and EB, the peak laminar flame speed of EA decreased as the initial temperature increased when compared to gasoline. At 60°C the difference in the peak laminar flame speed between gasoline and EA was 2.9cm/s, whilst at 120°C it was 3.845cm/s.

The laminar burning velocity proved to have good relation to the equivalence ratio and initial temperature of the reactants, as expected by theory [33–35]. Figure.10 shows that the laminar burning velocities for all the fuels increased as the initial temperature increased. For EP, EB and EA, the laminar burning velocities near the peaks at 120°C were approximately 6–8.5 cm/s faster than the results at 90°C, and approximately 4.6 –7 cm/s faster than the results at 60°C. At higher equivalence ratios, the difference between burning velocity for EP and EB were smaller at all examined initial temperatures, and their laminar burning velocities were similar to gasoline.

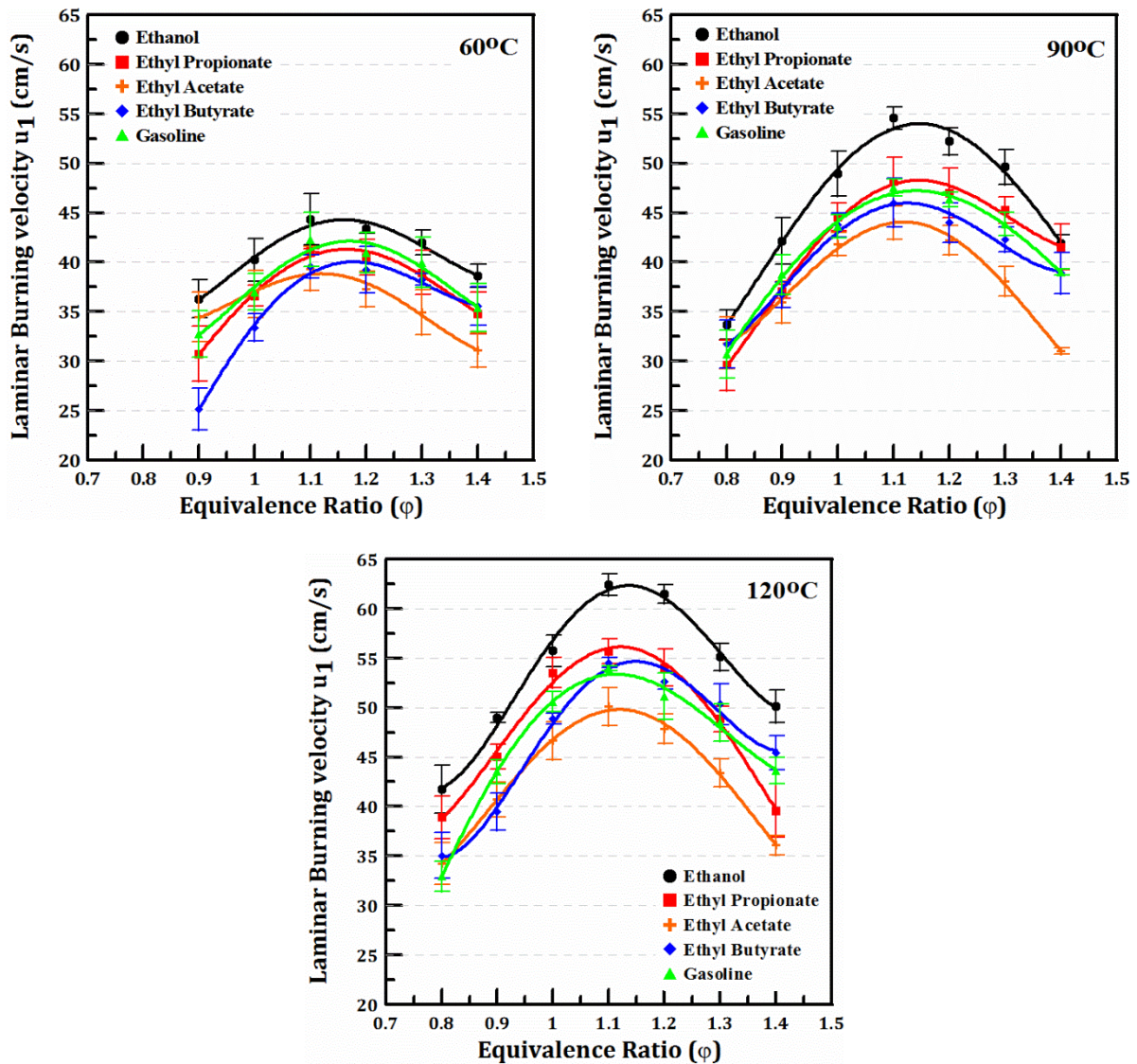


Figure.10. Laminar burning velocities of test fuels at different temperatures and equivalence ratios

In order to explain the results, the influence of molecular structure on the different laminar burning velocities was discussed. The highest laminar flame speed for ethanol could be due to its molecular structure, which consisted of hydroxyl functional group (-OH) attached to the terminal carbon atoms, leading to a higher laminar burning velocity compared to the other fuels [27, 36]. In the aspect of chemical kinetics, bond energy was used to investigate the flame speed difference among the ester fuel isomers. Gu et al. [27] demonstrated that isomers with more methyl groups have lower laminar flame speeds due to the high energy of the C-H bond in the methyl group. Ethanol had only one methyl group compared the ethyl ester fuels isomers which consists of two methyl group, thus leading to higher laminar flame speed for ethanol compared to ester fuels. The influence of the methyl group on the laminar flame speed for the ethyl ester fuels was eliminated due to their similar methyl group configuration.

Furthermore, dissociation bond energies of C-H on the terminal carbon atoms (terminal C-H) were larger than those of C-H on the inner carbon atoms (inner C-H) [27]. H atom was easily abstracted from the inner carbon atoms compared to that from the terminal carbon atoms. EP and EB had most inner C-H bonds compared to EA. Weak inner C-H bond energies in EP and EB facilitated the H-abstraction reaction compared to EA isomers, which had less inner C-H bonds. With more inner C-H bonds, EP and EB yielded the largest laminar burning velocity, whilst EA with minimum inner C-H bond displayed the smallest laminar burning velocity. The phenomenon of C-H bonds qualitatively agrees with the variation of laminar burning velocity, and this suggested that laminar burning velocities of ester isomers-air mixtures strongly depend on the bond dissociation energies.

Dayma et al. [28] investigated the sensitivity analyses of EP, EB and EA on the laminar flame speed at 0.1 MPa, 423 K, and equivalence ratios of 0.7, 1.0, and 1.4. They revealed that the most sensitive reaction, regardless of the equivalence ratio and the ester, was the branching reaction,  $H + O_2 \rightleftharpoons OH + O$ , which accelerated the flame. The sensitivity of this reaction increased with the equivalence ratio, and EA demonstrated slightly higher sensitivity compared to EP and EB. Moreover, they displayed that water formation by recombination of H and OH slowed the flame with a sensitivity slightly increasing with the equivalence ratio. EA demonstrated higher sensitivity to the water formation which slowed its laminar flame speed compared to EP and EB. The minimum sensitivity for the water formation was noticed for EP.

Figure.11 shows the burning flux versus equivalence ratio for the five fuels at different initial temperatures. The laminar burning flux reveals the eigenvalue of the flame propagation, which was obtained by multiplying the laminar burning velocity with the density of the unburned mixture. The general trend was similar to that of laminar burning velocity, where laminar burning velocity was the main influencing factor. However, the larger density of the EP-air mixture in comparison to the gasoline-air mixture contributed to a larger burning flux at all examined initial temperatures. At 90°C, EB demonstrated a similar trend to gasoline, whilst at 120°C it proved higher for  $\Phi > 1.1$ . Among the five fuels, ethanol yielded the highest laminar burning flux, whilst EA had the lowest. The peak values of all the fuels at the three temperatures existed between equivalence ratios of 1.0 and 1.2. Furthermore, with respect to temperature, the laminar burning flux of all the fuels increased as the initial temperature increased.

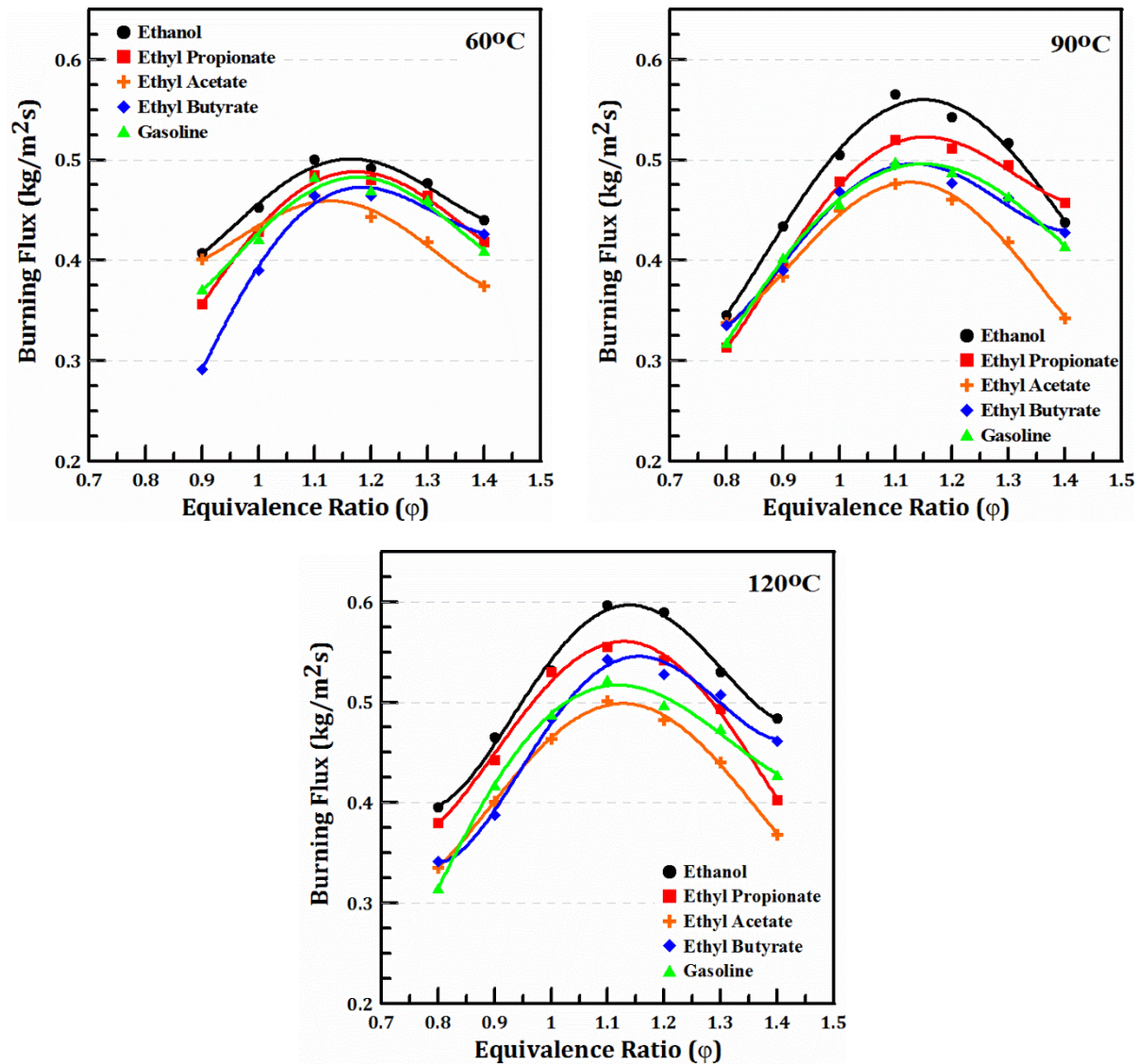


Figure.11. Burning flux of test fuels at different temperatures and equivalence ratios (a) 60°C, (b) 90°C and (c) 120°C

## Conclusions

Laminar combustion characteristics of ethanol, gasoline, EP, EB and EA–air mixtures were investigated using high-speed schlieren photography at initial temperatures of (60°C, 90°C and 120°C) over wide range of equivalence ratios ( $\phi = 0.8$ -1.4) under 0.1 MPa initial pressure in a constant volume vessel. The characteristics of the ethyl ester fuels were compared to the cases of ethanol and gasoline. The main conclusions are summarized as follows:

1. The un-stretched flame speeds of EP, EB and EA were lower than that of ethanol and gasoline at an initial temperature of 60°C. As the initial temperature increased to 90°C and 120°C, the un-stretched flame speeds of EP also increased, relative to gasoline. At 120°C, the un-stretched flame speeds of EB increased compared to gasoline, especially for rich conditions. EA consistently displayed the lowest un-stretched flame speeds among the five fuels.

2. The EB and EA flames proved more stable compared to ethanol and gasoline at equivalence ratios lower than 1.1 for 60°C and 120°C. EP demonstrated greater flame stability than ethanol, however less when compared to gasoline at equivalence ratios lower than 1.0, at all examined temperatures. The flame thickness results showed that EB and EA presented a lower hydrodynamic instability performance among the five fuels for most of the test points. The Markstein numbers displayed similar trends as the Markstein lengths for the current tests.

3. The laminar burning velocities of the EP fuels proved faster compared to EB and EA, whilst slower compared to ethanol and gasoline at 60°C. As the initial temperature increased, up to 120°C, the laminar flame speed of EP and EB became faster, when compared to gasoline. The lowest laminar burning velocity was observed for EA among all the five fuels. Moreover, at an initial temperature of 60°C the maximum burning velocity between the ethyl ester fuels proved similar (at 0.1 MPa, 41.2 cm/s for EP, 39.6 cm/s for EB and 39.4 cm/s for EA). However, at higher initial temperatures (120°C), the maximum burning velocity remained close between EP (55.7 cm/s) and EB (54.52 cm/s), but not when compared to that of EA (50.1 cm/s).

The results of this investigation showed that ethyl ester fuels demonstrated robust combustion characteristics, especially EP and EB, when compared to ethanol and gasoline. For future work, a detailed study of the effect of

ethyl ester fuels on the engine performance and emissions in Gasoline Direct Injection (GDI) engine would ensure an enhanced consideration of the advantages of ethyl ester fuels as surrogate fuels for gasoline.

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### Paper Abbreviations

RON	Research Octane Number	EA	Ethyl acetate
EP	Ethyl propionate	EB	Ethyl butyrate
2MF	2-methylfuran	2,5DMF	2, 5-dimethylfuran
DFB	dual fermentation bio-refinery	SI	Spark ignition
CI	Compression ignition	HCCI	Homogeneous charge compression ignition
PRF95	Primary Reference Fuels	$S_n$	Stretched laminar flame speed
$r_u$	Instantaneous flame radius	$\alpha$	Stretch rate
$L_b$	Markstein length	$S_s$	Unstretched laminar flame speed
$\rho_b$	Burned mixture densities	$\rho_u$	Unburned mixture densities
$n_u$	Number of reactant moles	$n_b$	Number of product moles
$T_u$	Initial temperature	$T_b$	Adiabatic flame temperature
$\nu$	kinematic viscosity	$u_l$	Laminar burning velocity
LHV	Lower heating value	$\delta_L$	flame thickness
Ma	Markstein number	$f$	laminar burning flux
$\phi$	Fuel-air equivalence ratio		

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